

MTH 111

Answer Key to the Practice Problems for Exam 1

I

1.

- (a) $f(0) = 3$; (b) $f(2) = 4(2)^2 - 2 + 3 = 16 - 2 + 3 = 17$.
(c) $f(-2) = 4(-2)^2 - (-2) + 3 = 4 \cdot 4 + 2 + 3 = 16 + 2 + 3 = 21$.
(d) $f(-x) = 4(-x)^2 - (-x) + 3 = 4x^2 + x + 3$; (e) $f(t) = 4t^2 - t + 3$
(f) $f(2-t) = 4(2-t)^2 - (2-t) + 3 = 4(4 - 4t + t^2) - 2 + t + 3 = 4t^2 - 15t + 17$

2.

- (a) $g(-5) = 0$; (b) $g(2)$ undefined, since we cannot divide by 0.
(c) $g(x+h) = \frac{x+h+5}{x+h-2}$; (d) $g(1-a) = \frac{(1-a)+5}{(1-a)-2} = \frac{6-a}{-1-a} = \frac{a-6}{a+1}$

3.

- (a) All real numbers; (b) All real numbers except 0;
(c) All real numbers except -1 and 1 .

II

1

- (a) Equation: $y = -3x + 5$
(b) Slope: $m = \frac{2-0}{-2-2} = \frac{2}{-4} = -\frac{1}{2}$. This gives $y - 0 = -\frac{1}{2}(x - 2)$ or
 $y = -\frac{1}{2}x + 1$
(c) The slope of the line is 3, so using the point-slope equation, we get
 $y - 1 = 3(x + 1)$ i.e. $y = 3x + 4$
(d) Let m be the slope. Then $3m = -1$, so $m = -\frac{1}{3}$

The point-slope equations gives $y - 1 = -\frac{1}{3}(x + 1)$. That is $y = -\frac{1}{3}x + \frac{2}{3}$

2.

- (a) Solving for y we get $y = 2x + 2$. So the slope is 2 and the y -intercept is 2 or $(0, 2)$.
(b) Solving for y , we get $y = -\frac{3}{4}x + 2$. The slope is $-\frac{3}{4}$ and the y -intercept is 2 or
 $(0, 2)$

III

1. #24, page 117

Let h be the height of the triangle. Then its base is $2h - 7$. Let A be its area, then

$$A = \frac{h(2h - 7)}{2}.$$

2. (a) $(f + g)(4) = f(4) + g(4) = (2(4)^2 + 1) + (4 - 2) = 32 + 1 + 4 - 2 = 35$

(b) $(f - g)(0) = 1 - (-2) = 3$

(c) $(fg)(-1) = f(-1)g(-1) = (2(-1)^2 + 1)(-1 - 2) = 3(-3) = -9.$

(d) $\left(\frac{f}{g}\right)(4) = \frac{f(4)}{g(4)} = \frac{2(4)^2 + 1}{4 - 1} = \frac{33}{2}$

(e) $\left(\frac{f}{g}\right)(2) = \frac{f(2)}{g(2)}$ not defined since we can divide by 0.

3. (a)

Domain of f : all real numbers.

Domain of g : All nonnegative real numbers (positive and 0).

Domain of $f + g$: All nonnegative real numbers.

Domain of $f - g$: All nonnegative real numbers.

Domain of fg : All nonnegative real numbers.

Domain of ff : All real numbers.

Domain of f/g : All positive real numbers.

(b)

$$(f + g)(x) = f(x) + g(x) = x^2 + \sqrt{x}; \quad (f - g)(x) = f(x) - g(x) = x^2 - \sqrt{x}$$

$$(fg)(x) = f(x)g(x) = x^2\sqrt{x}; \quad (ff)(x) = f(x)f(x) = (x^2)(x^2) = x^4.$$

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{x^2}{\sqrt{x}}.$$

4.

$$\frac{f(x+h) - f(x)}{h} = \frac{[3(x+h)^2 - 2(x+h)] - [3x^2 - 2x]}{h} = \frac{3(x^2 + 2xh + h^2) - 2x - 2h - 3x^2 + 2x}{h}$$

This yields

$$\frac{f(x+h) - f(x)}{h} = \frac{6xh - 2h + h^2}{h} = \frac{h(6x - 2 + h)}{h} = 6x - 2 + h$$

IV

1.

33, page 135

We get

$$f(-x) = -3(-x)^3 + 2(-x) = -3(-1)^3 x^3 - 2x = 3x^3 - 2x = -(-3x^3 + 2x) = -f(x).$$

So this is an odd function.

#34, page 135

$$f(-x) = 7(-x)^3 - 4x - 2 = -7x^3 - 4x - 2$$

This neither an even function nor an odd function.

#35, page 135

$$f(-x) = 5(-x)^2 + 2(-x)^4 - 1 = 5x^2 + 2x^4 - 1 = f(x).$$

So this is an even function..

#40, page135: Neither

42, page135: Even function

#45, page135 : Horizontal shift of the graph of the function $y = x^3$ by 5 units to the left.

#54, page136, Reflection of the graph of the function $y = x^3$ across the x-axis, then shifted up by 5 units.

2.

2, page 144:

$$y = kx \text{ and } 0.1 = 0.2k. \text{ Thus } \frac{0.1}{0.2} = \frac{1}{2}, \text{ i.e. } y = \frac{1}{2}x.$$

6, page 144:

$$y = \frac{k}{x} \text{ and } 0.1 = \frac{k}{0.5}. \text{ This yields } k = 0.1(0.5) = 0.05.$$

$$\text{Thus } y = \frac{0.05}{x}$$

16, page 136

$$\text{We have } t = \frac{k}{r}. \text{ When } r = 80, t = 5. \text{ Thus } 5 = \frac{k}{80}, \text{ that is } k = 400.$$

$$\text{We get } t = \frac{400}{r}.$$

$$\text{If } r = 70, \text{ we get } t = \frac{400}{70} \approx 5.71 \text{ hrs, about 4 hours and 43 minutes}$$